

# Treatment of Epistemic Uncertainty in PSHA Results

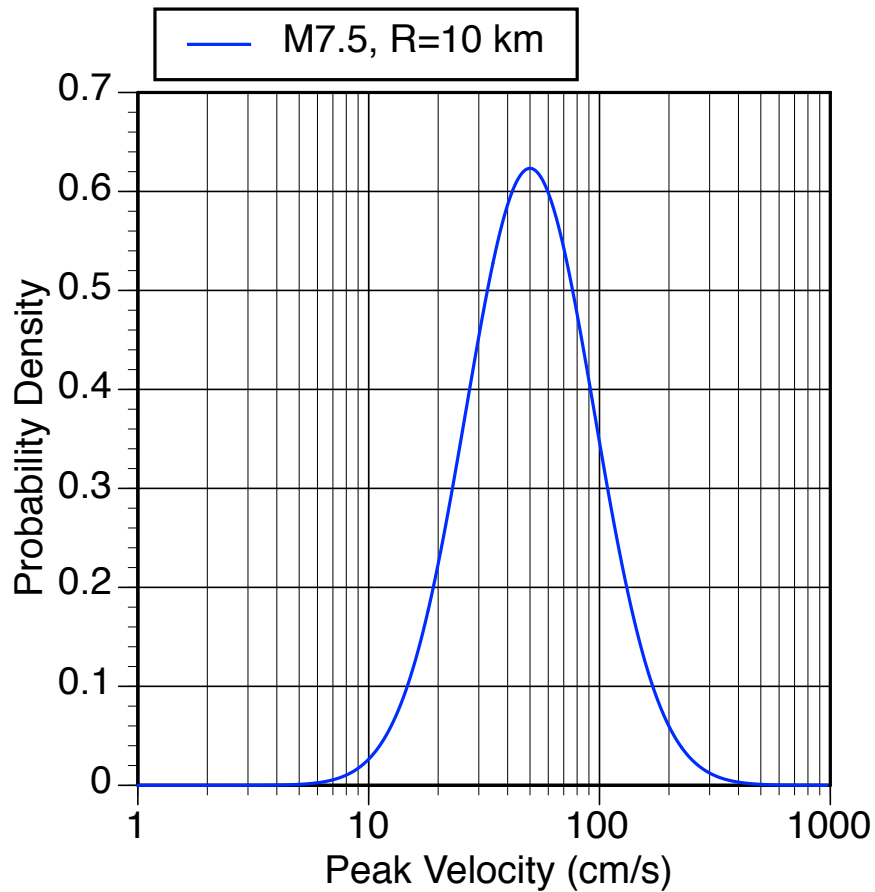
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PSHA Workshop, Lenzburg, Switzerland, Sep 7, 2017

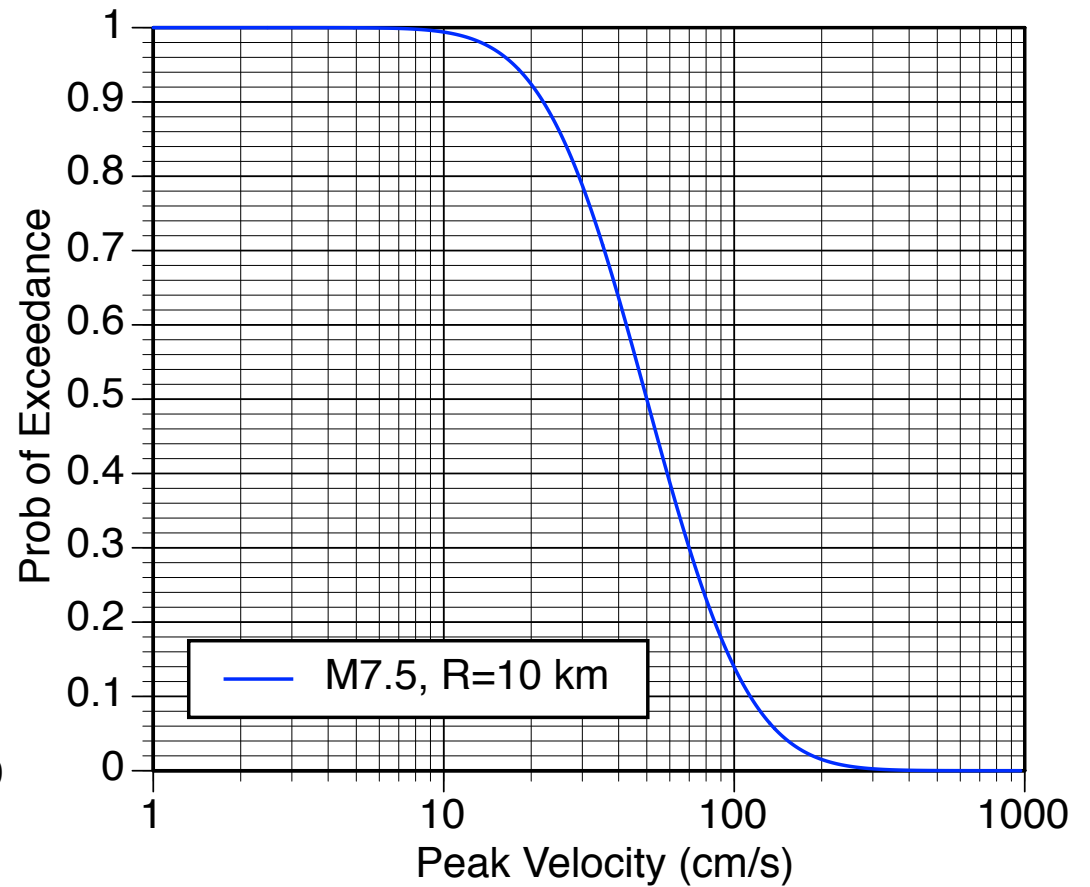
$$Haz(GM > z) = \sum_{i=1}^{N_{scenarios}} Rate(Scenario_i) P(GM > z | Scenario_i)$$

- Scenario
  - Magnitude
  - Mechanism
  - Rupture Dimension
  - Rupture Location

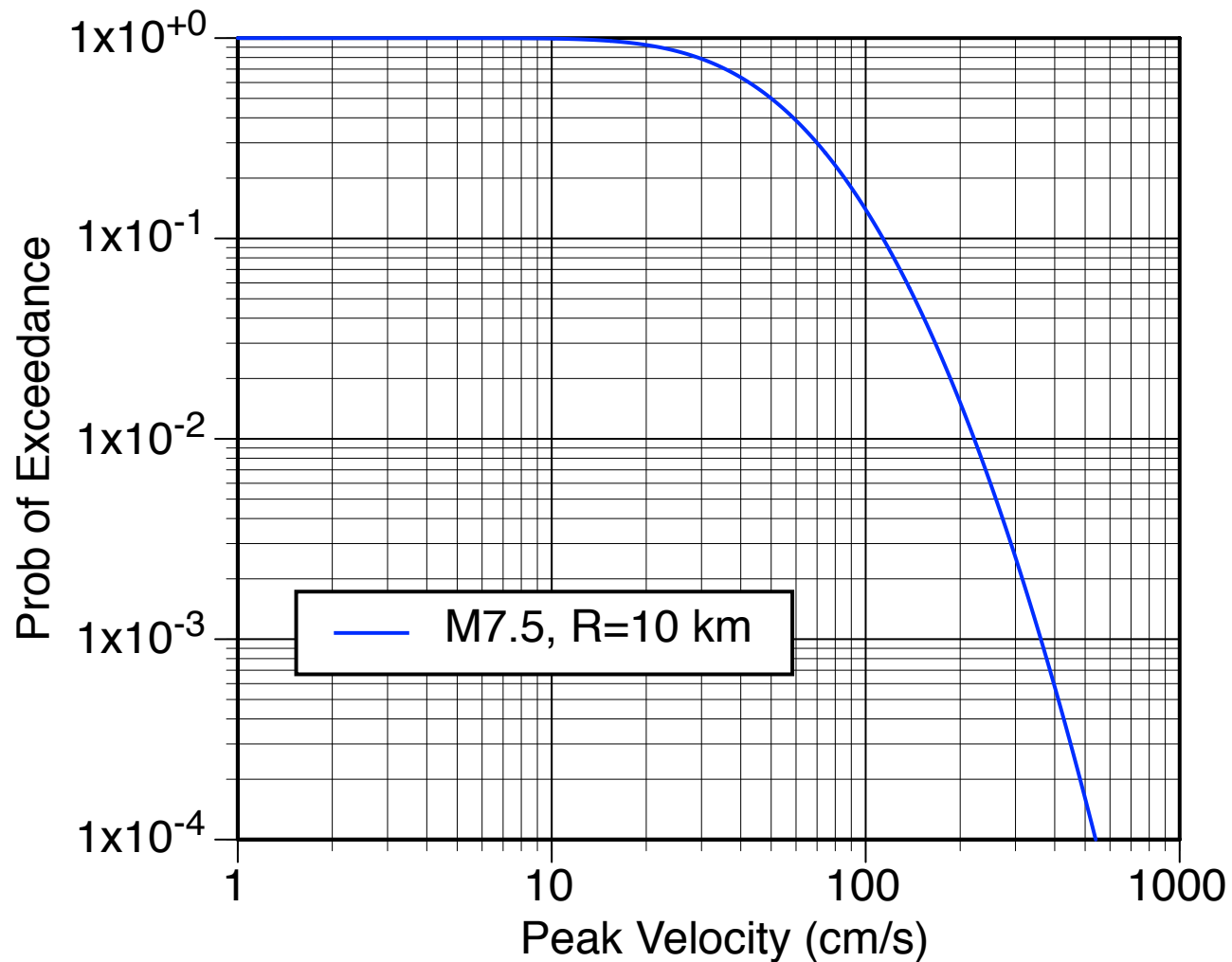
# PGV Distribution



$$P(GM > z | Scenario_i)$$



# Select Appropriate Ground-Motion Probability Level



# Select Appropriate GM Probability Level (for a single scenario)

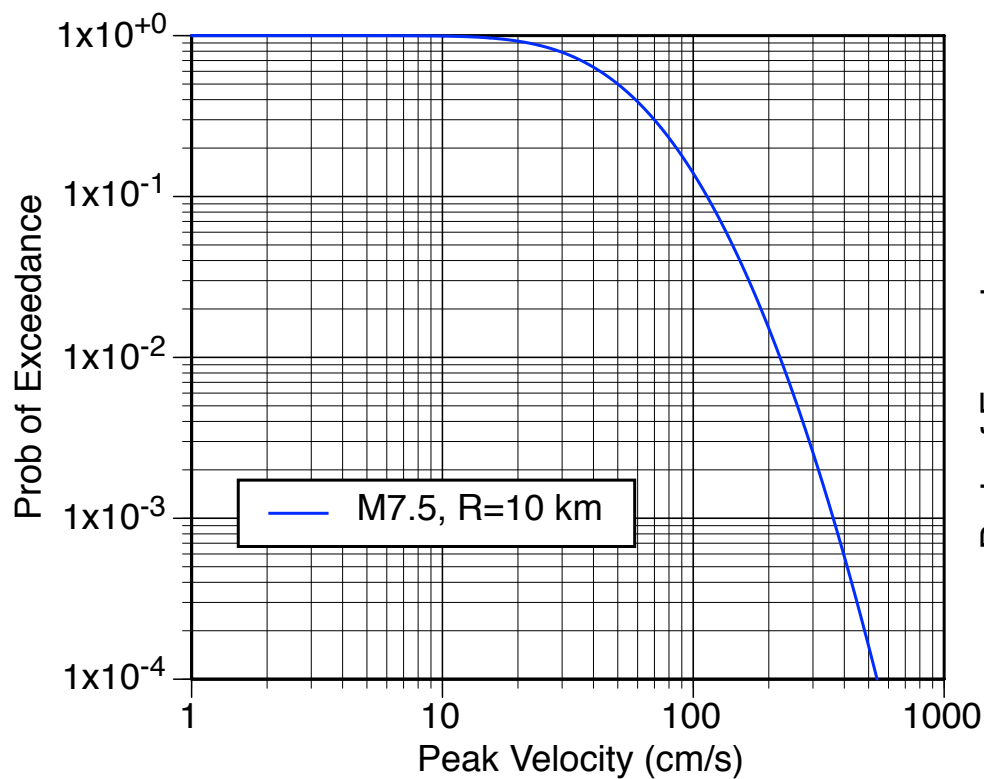
- Deterministic Seismic Hazard
  - Choose a probability level for the number of standard deviations (epsilon) of the ground motion:

$$P(PGV > z \mid M, R)$$

- Probabilistic Seismic Hazard
  - Choose a probability level for the combined chance of the earthquake occurring and the number of standard deviations of the ground motion:

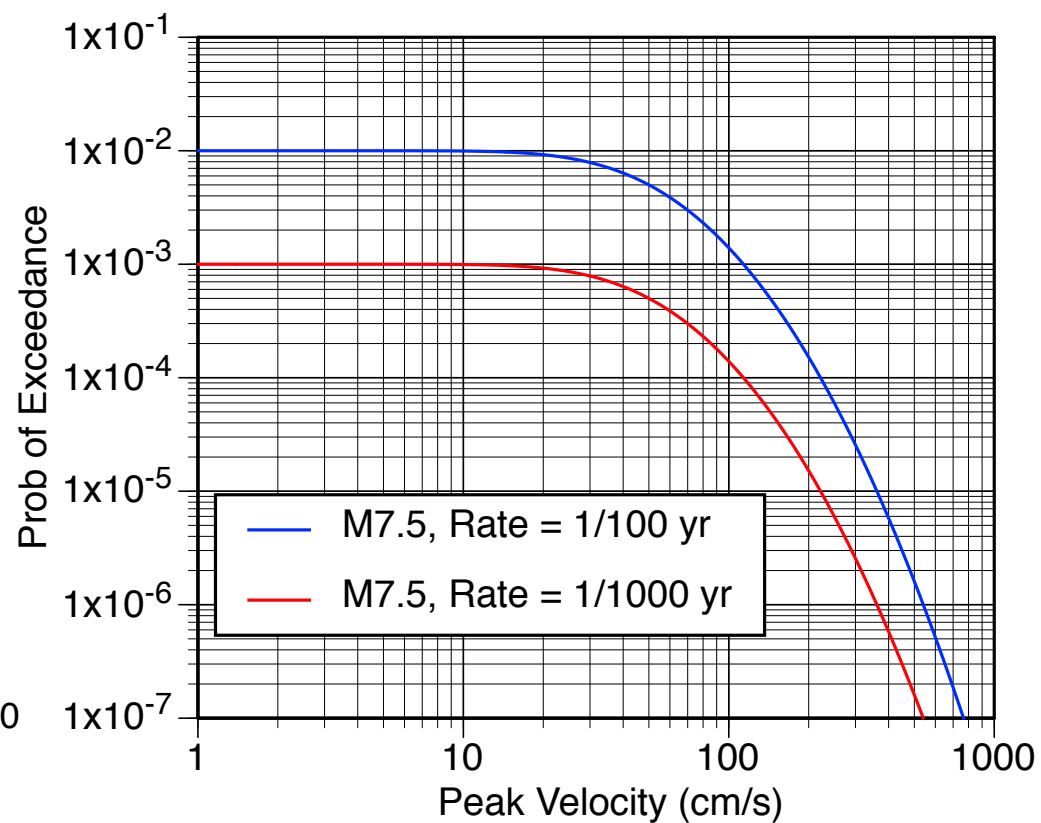
$$\text{Rate}(eqk) * P(PGV > z \mid M, R)$$

# Deterministic

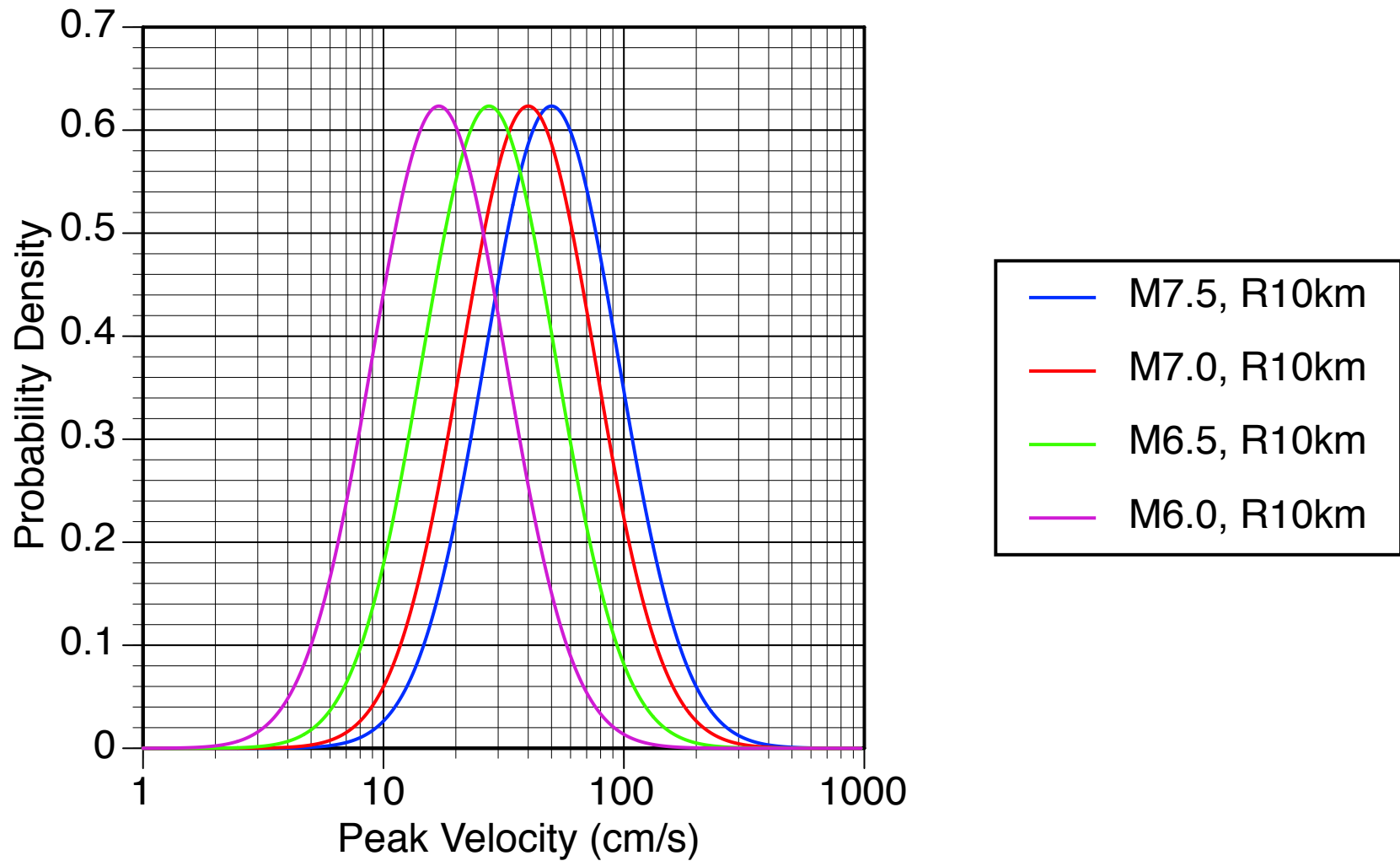


# Probabilistic

$$\text{Haz}(z) = \text{Rate}(\text{eqk}) * P(\text{PGV} > z | M, R)$$

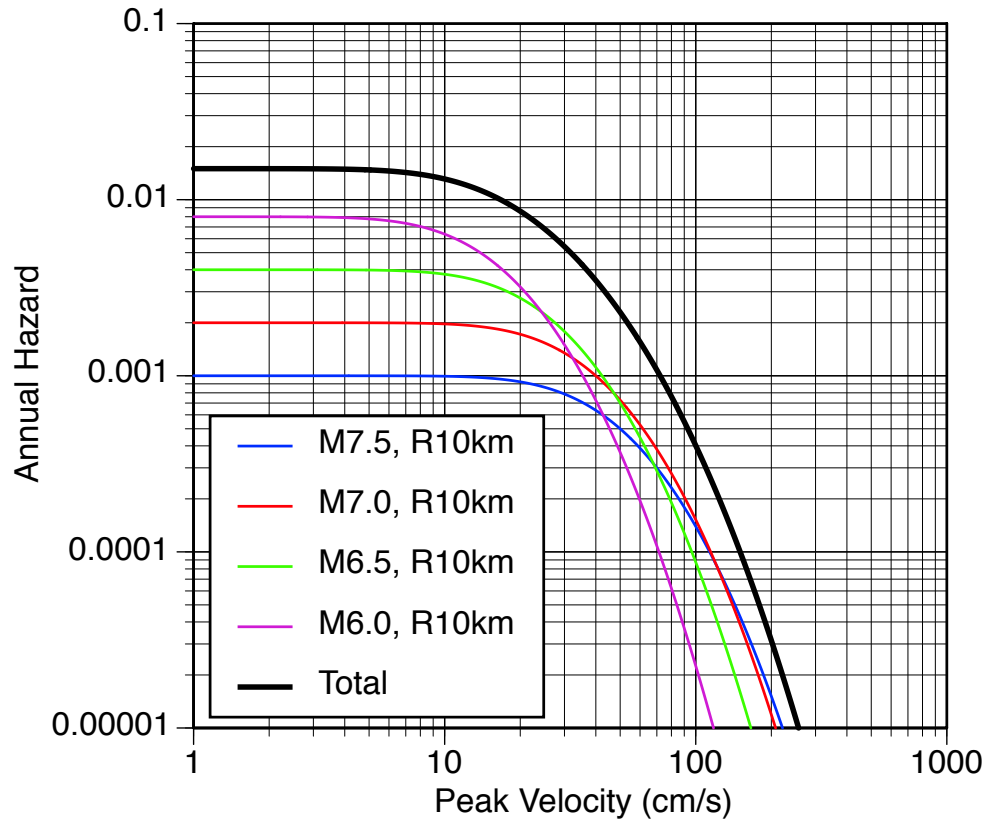
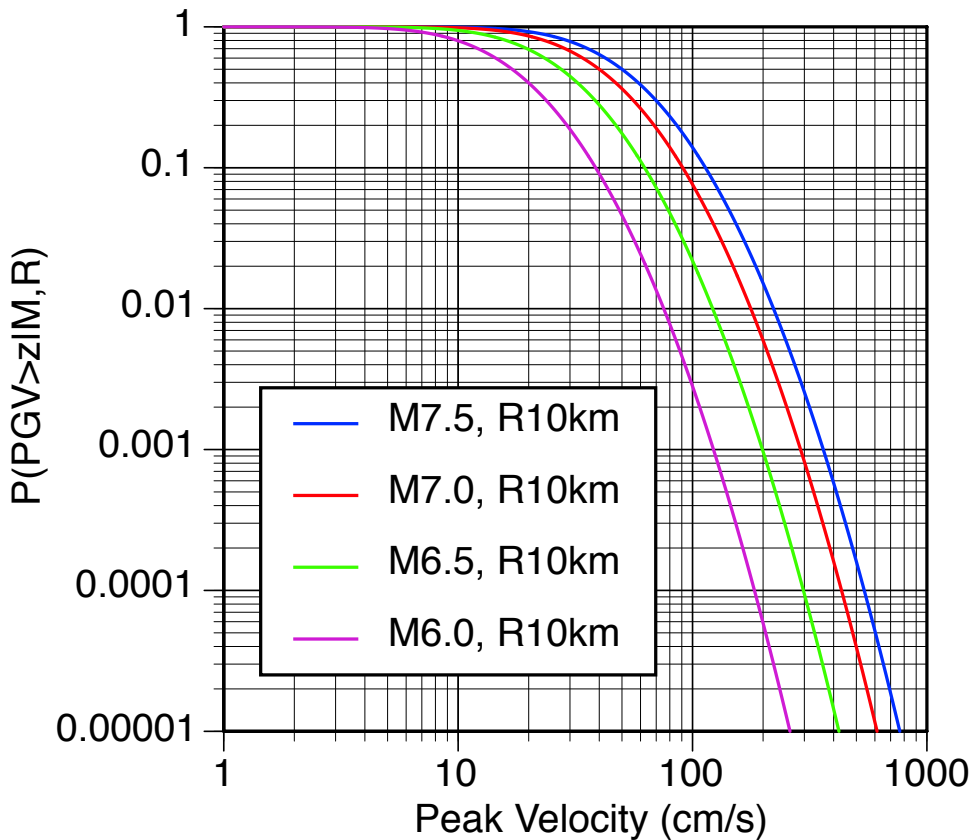


# Large Variability Leads to Overlaps of Ground Motion Distributions



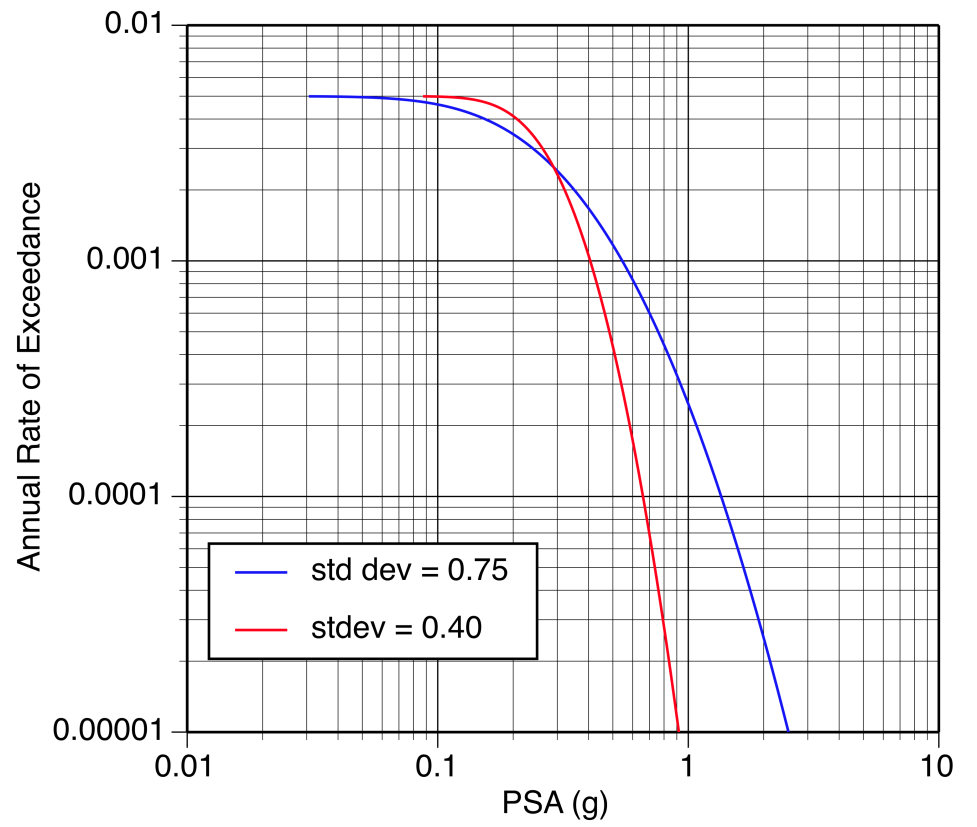
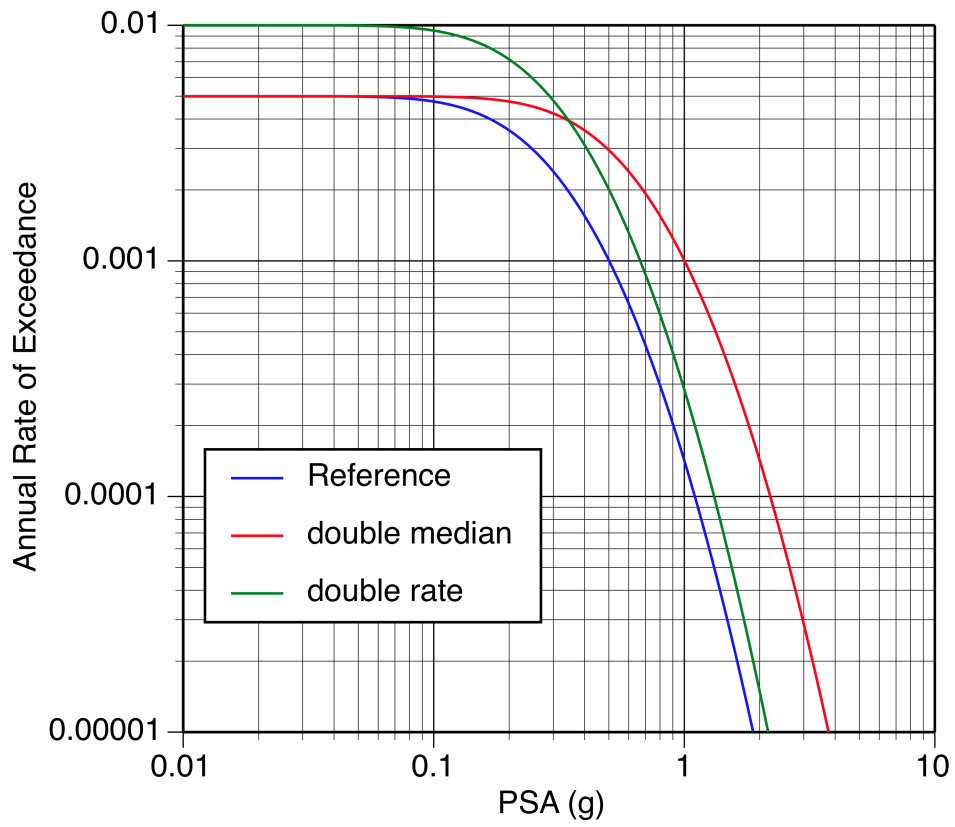
# Multiple scenarios

$$Haz_z(PGV > z) = \sum_{i=1}^{N_{Scenario}} Rate_i P(PGV > z | M_i, R_i)$$

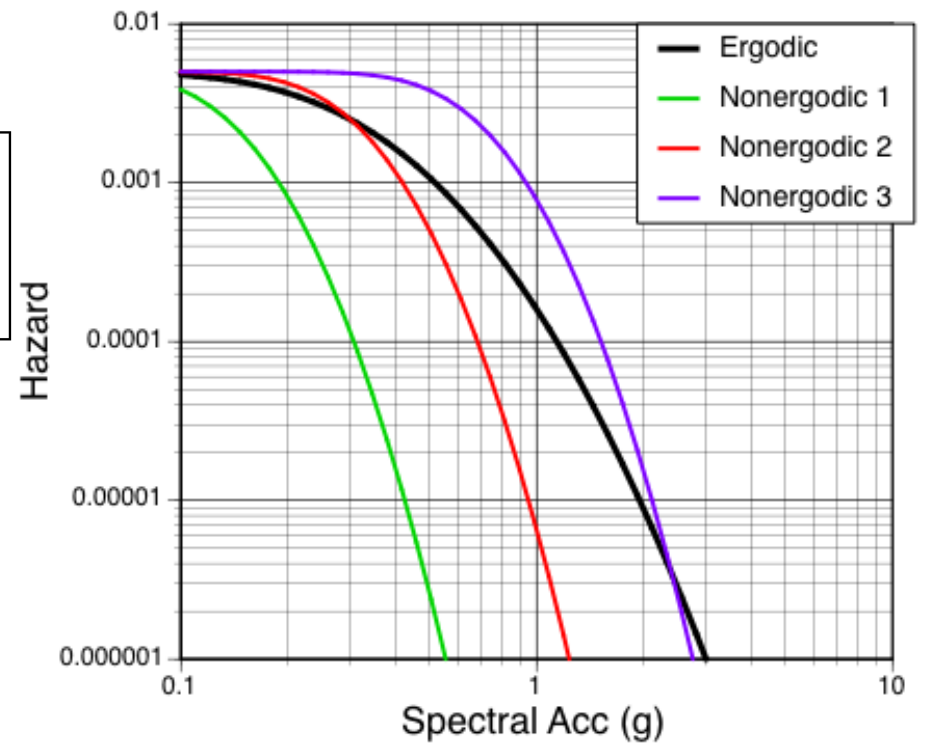
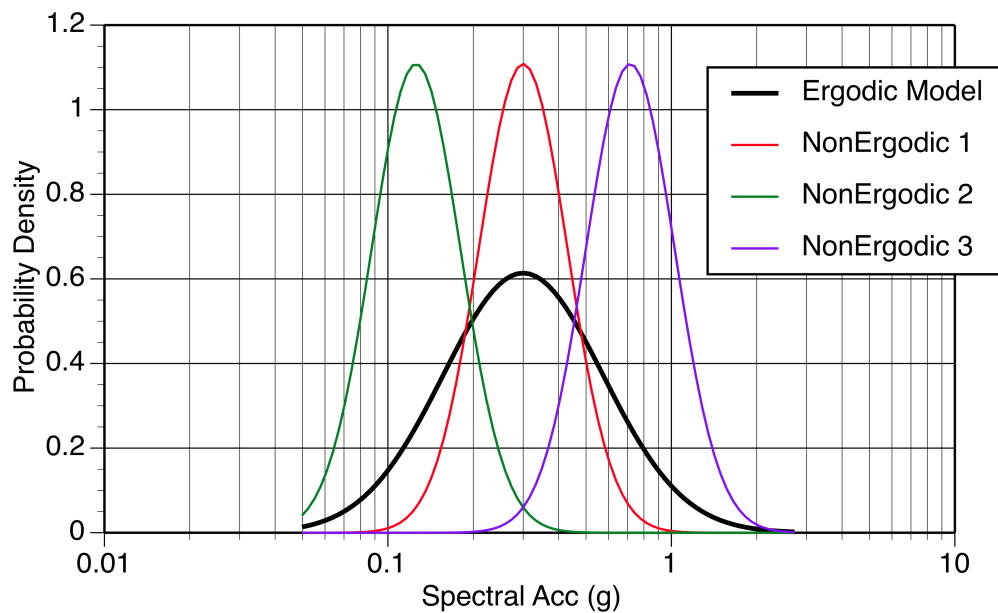




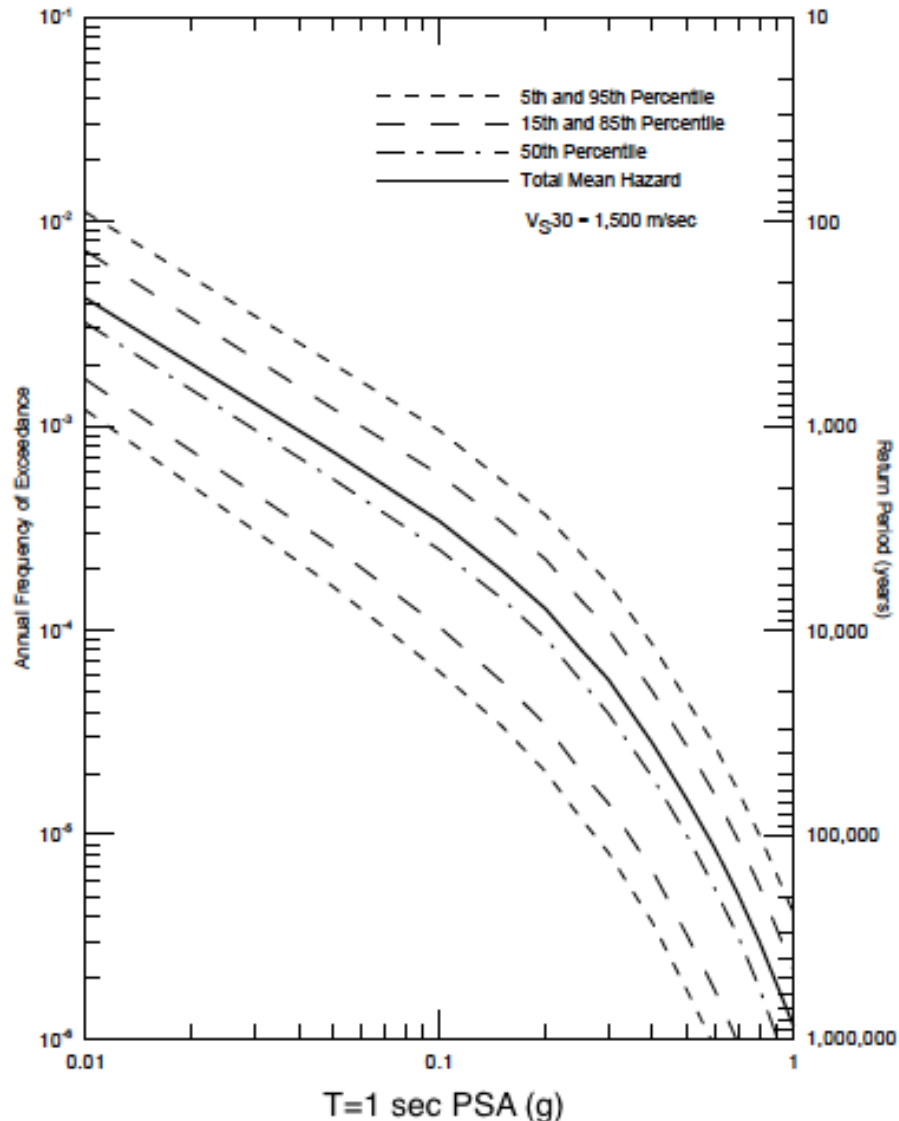
# Hazard Sensitivity



# Epistemic Uncertainty for Nonergodic GM Models



# Example Uncertainty in Hazard

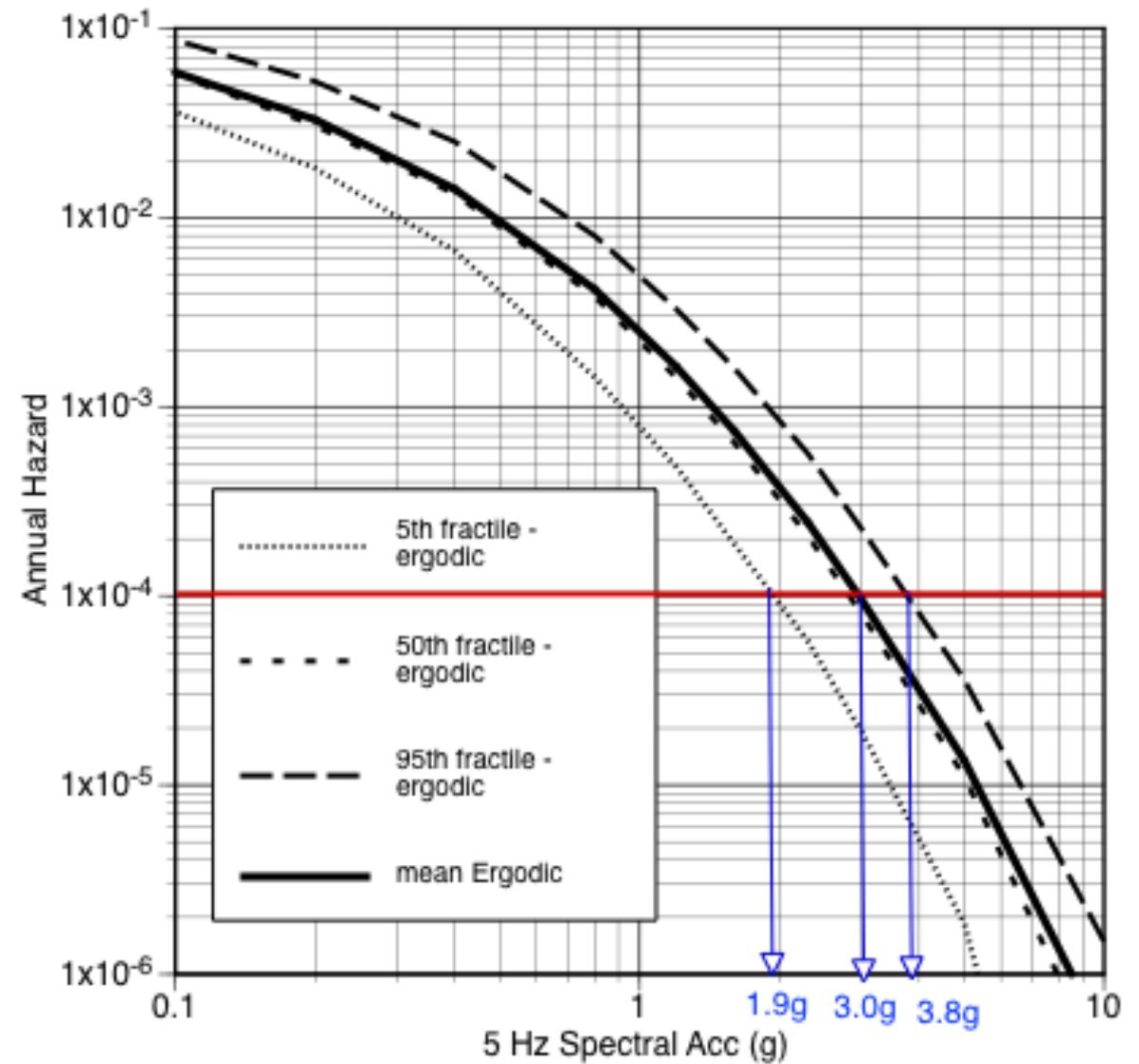


- Full range of hazard curves is the result
- Need to choose a design ground motion from this range of curves
  - How safe do you want to be?
  - How confident do you want to be in the level of safety?
  - Mean hazard is selected for engineering application
  - Mean hazard it is not a forward prediction of rate of ground motions

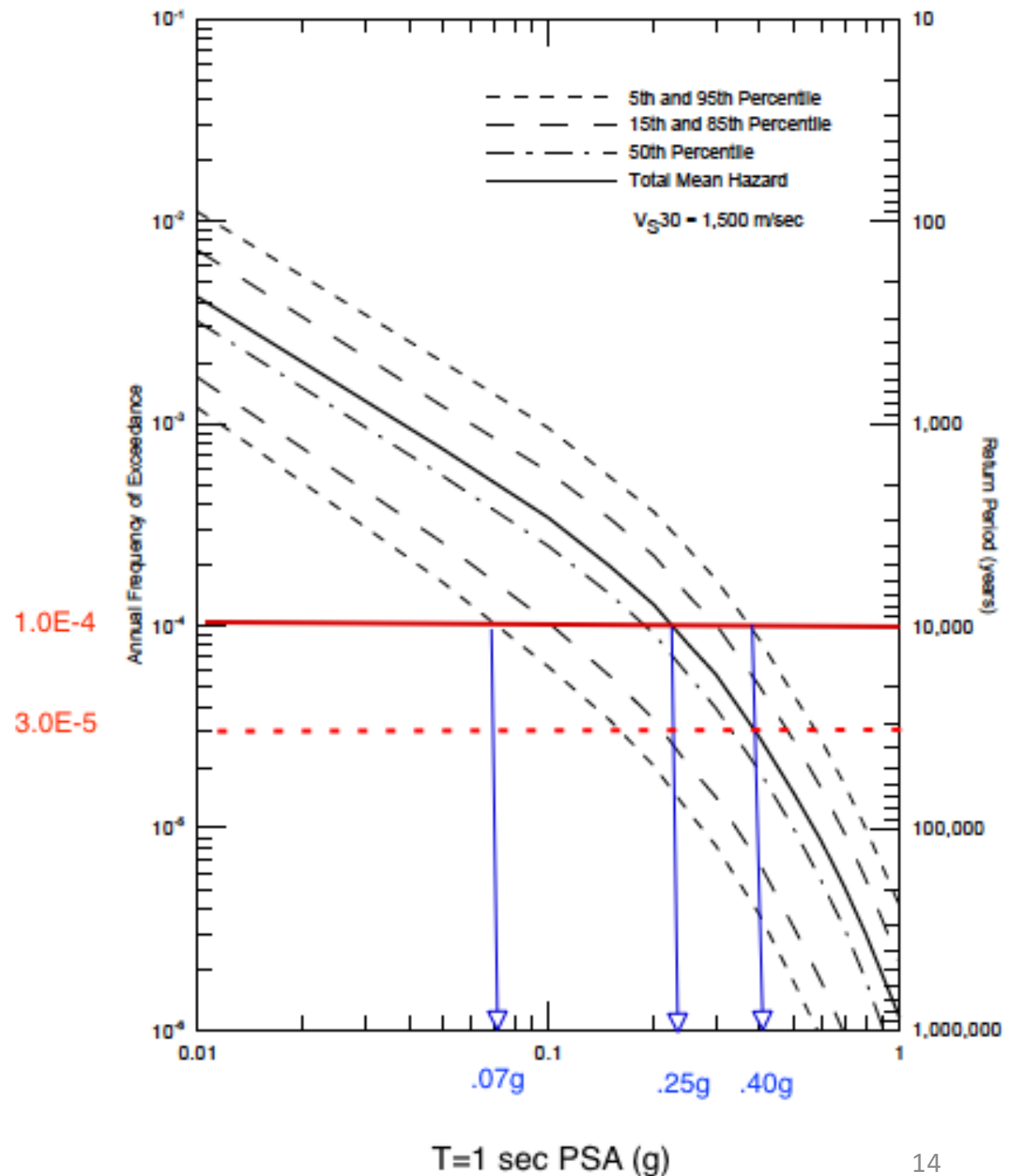
# Why use Mean Hazard?

- Used for Mean Risk
  - The mean hazard curve combined with the mean fragility curves leads to mean risk
- Mean Penalizes large uncertainty
  - Distribution of fractiles is skewed to high end (close to log normal)
  - For larger uncertainty, mean will be at a higher fractile
- Disadvantage
  - It leads to changing fractile levels depending on the amount of uncertainty and the selected return period
  - If only the mean is shown, then don't know the fractile level

# Example PSHA for San Jose (high activity)



# Example PSHA for Colorado (low seismicity)



# Communicating Epistemic Uncertainties

- For critical facilities, epistemic uncertainties are shown in plots in the report, but summary tables of results often only show the mean hazard
- For better communication
  - The uncertainties should be included in all tables of results and in the executive summary

# Uses of Epistemic Uncertainty

- Show the limitations of the current earthquake science to constrain the seismic hazard
  - Consider the uncertainty of the design ground motion when making engineering judgments
  - This can change engineering judgments
- Use a hazard fractile for the design ground motion rather than the mean hazard
  - e.g. select the 85<sup>th</sup> fractile
  - Unlikely to be adopted
- Use the ground motion from a higher fractile (90<sup>th</sup>) to check the design
  - Don't apply design criteria limits, but avoid catastrophic failure

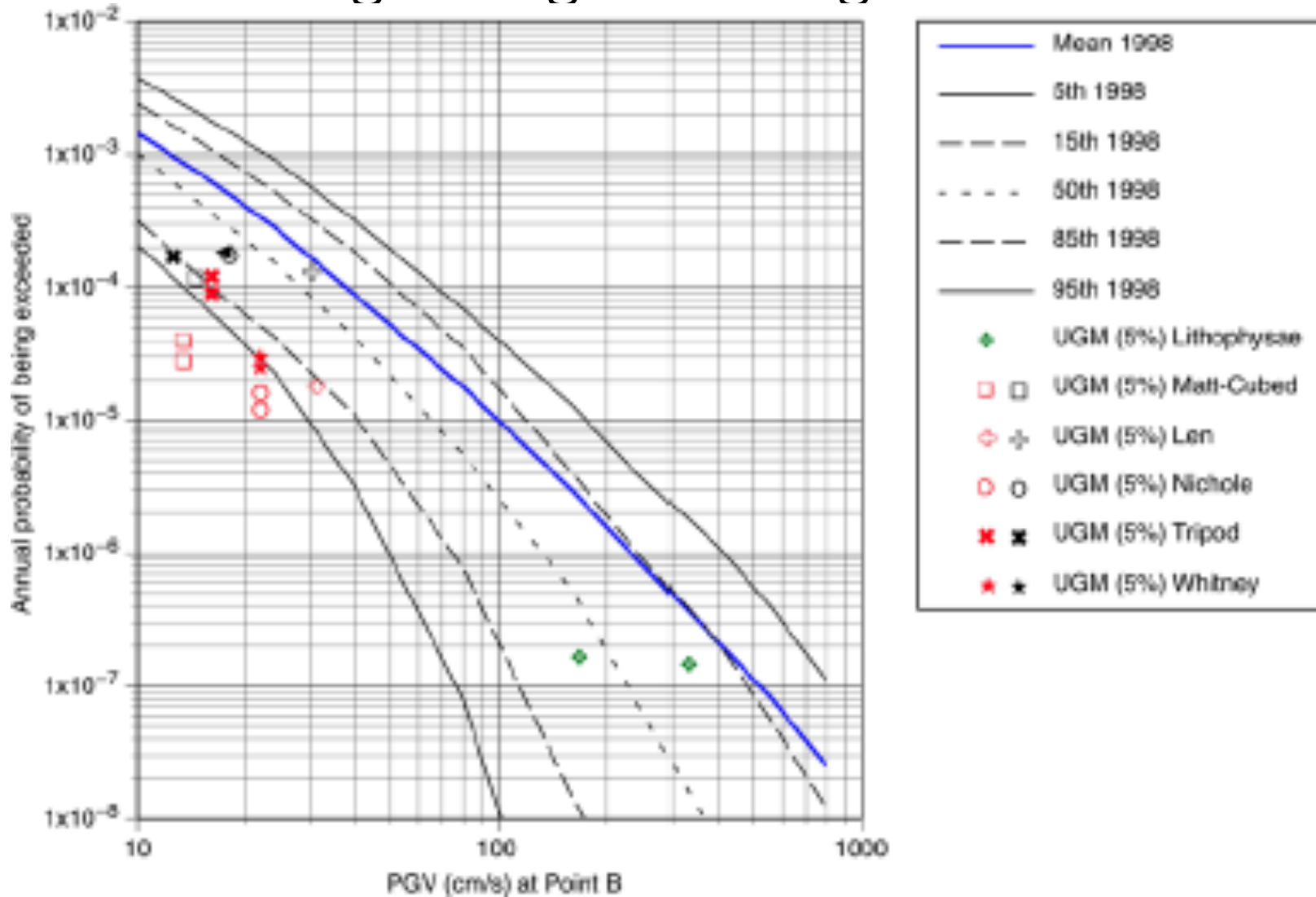


# Uses of Epistemic Uncertainty - Retrofits

- Once the decision is made to retrofit, then a goal is not to have to retrofit again in short time (10 years).
- Consider designing the retrofit for a higher fractile instead of the mean
  - Use 90<sup>th</sup> fractile to have confidence that the retrofit will not be found inadequate when the hazard is updated.

# Example:

Use of precarious rock information at Yucca Mtn to change weights on logic tree branches



# Underestimation of Epistemic Uncertainty

- Epistemic uncertainty is due to lack of data
  - Less data implies larger uncertainty
- In practice, not always the case
  - Typically estimated using alternative available models/data
  - Few available studies lead to small uncertainty (few alternatives available)
  - Many available studies lead to larger uncertainty (more alternatives available)
- Often, our estimate of the epistemic uncertainty increases the more studies we do, indicating that the epistemic uncertainty tends to be underestimated when we have little information

# Additional Epistemic Uncertainty (missing from current PSHA studies)

- **Nonergodic GMPEs**
  - New data sets with large number of earthquakes and recordings shows the size of the systematic source, path, and site effects
  - Most of the standard deviation in traditional GMPEs is from systematic effects, not random
    - Ergodic standard deviation is about 0.65 LN units
    - Removing systematic site, path, and source: 0.4 LN units

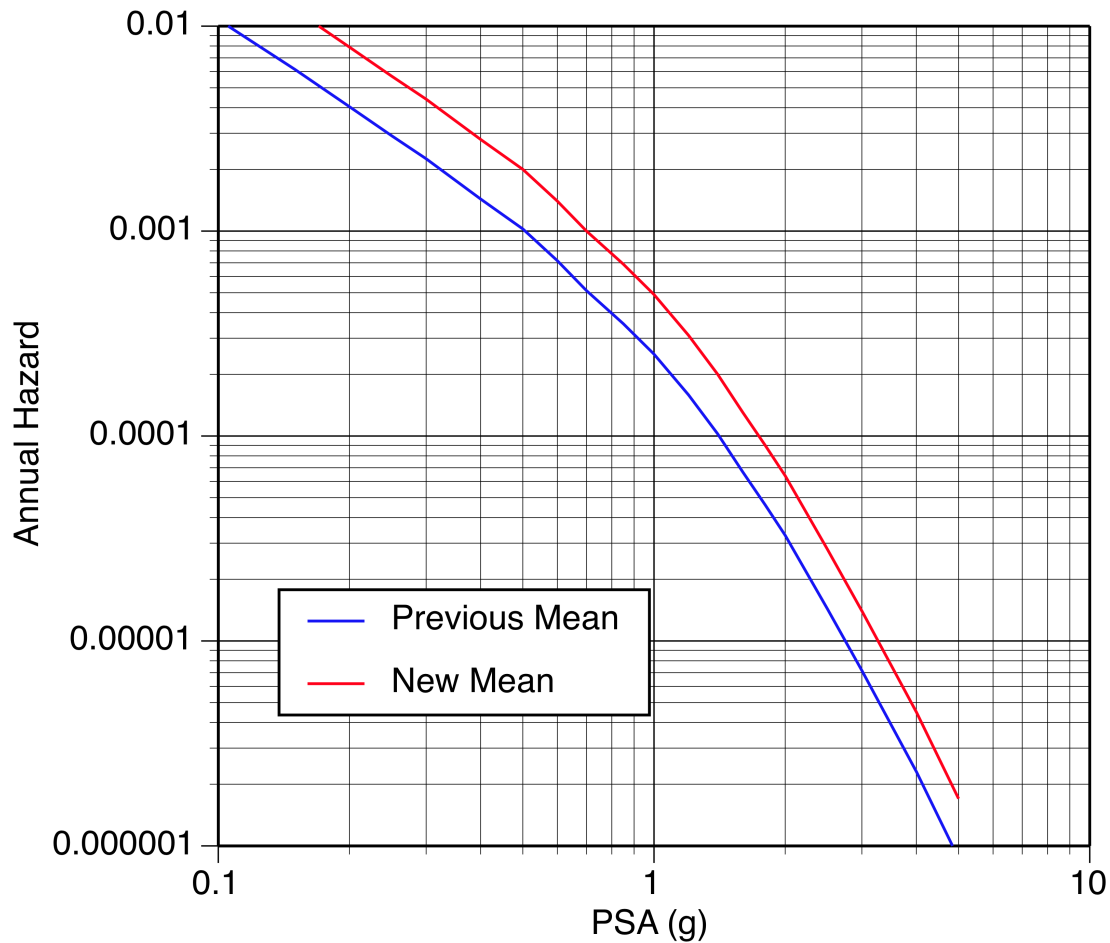
# Additional Epistemic Uncertainty (continued)

- Nonergodic GMPEs
  - We now know how far off our global models can be for a site-specific application
  - In most cases, the systematic path and source effects are currently not well constrained
    - In the short term, expect to see a significant increase in epistemic uncertainty
  - Highlights the need to collect additional ground motion data and to develop of 3-D crustal models for use in numerical simulations of path effects
  - Business case for seismic instrumentation

# Hazard Uncertainty and Stability of Results for Building Codes

- Need for stability of the design ground-motion maps for building codes
- Expect significant changes in the hazard results
  - Large epistemic uncertainties
  - Significant changes can be expected as new data are collected and new methods and models are developed
- What is an insignificant change?

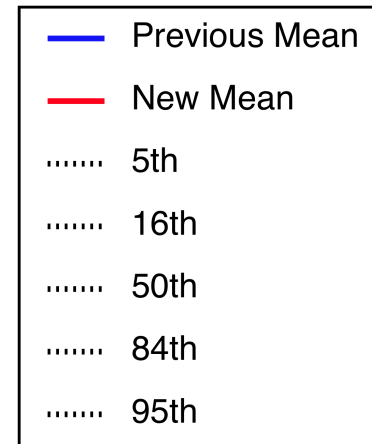
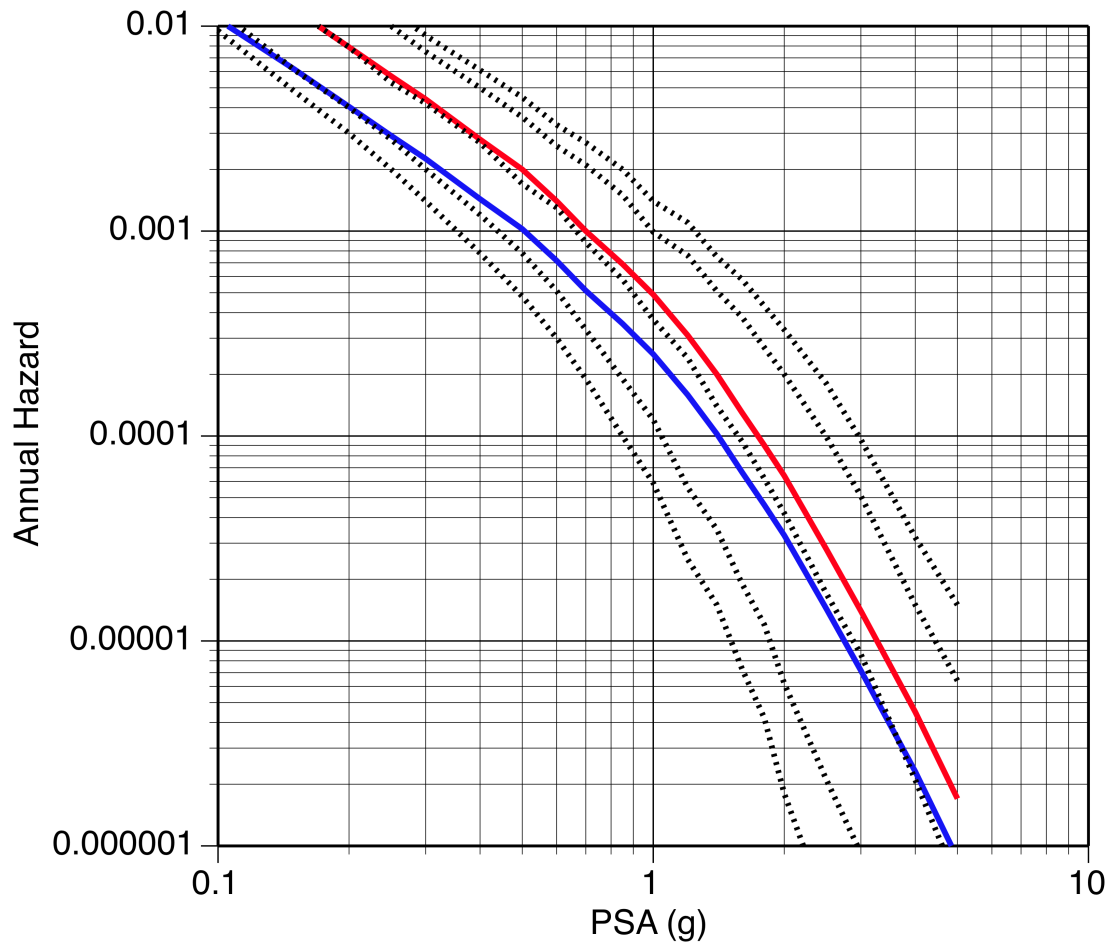
# Example of Change in Mean Hazard



20% increase in  $1E-4$  UHS  
Are we confident in the change?

Should the building code  
values be revised?

# Change in Mean Hazard Considering Epistemic Uncertainty



25% increase in 4E-4 UHS  
Are we confident in the change?

Look at the epistemic uncertainty range



# Stability and Consideration of New Data & Models

- Need to decide when an update of the hazard is justified
- Is the change robust given the uncertainty in the earthquake science?

$$Is \ln \left( \frac{UHS\_new(T)}{UHS\_old(T)} \right) > 0.5 \sigma_{\ln UHS}(T) ?$$

*Is  $UHS\_old(T)$  outside of the updated 25th-75th fractiles ?*

# Conclusions

- Large epistemic uncertainties in seismic hazard
  - This is the main limitation of PHSA, but it also is a key limitation of Deterministic approaches
- The epistemic uncertainty should be communicated to the engineers using the results
  - Consider GM epistemic uncertainty along with other uncertainties when making engineering judgments
  - Demonstrates the need for long-term research to reduce the uncertainty in the inputs to PSHA models
- The prediction from PHSA is the range of the uncertainty fractiles
  - Testing of PHSA results should consider the fractiles, not just the mean hazard